

Mathematica 11.3 Integration Test Results

Test results for the 46 problems in "1.1.3.6 (g x)^m (a+b x^n)^p (c+d x^n)^q (e+f x^n)^r.m"

Problem 7: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (A + B x^n) (c + d x^n)}{(a + b x^n)^3} dx$$

Optimal (type 5, 228 leaves, 3 steps):

$$\begin{aligned} & - \left((A b (b c (1+m-2n) - a d (1+m-n)) - a B (b c (1+m) - a d (1+m+n))) (e x)^{1+m} / \right. \\ & \quad \left. (2 a^2 b^2 e n^2 (a + b x^n)) + \frac{(A b - a B) (e x)^{1+m} (c + d x^n)}{2 a b e n (a + b x^n)^2} - \right. \\ & \quad \left. \left((b c (a B (1+m) - A b (1+m-2n)) (1+m-n) + a d (1+m) (A b (1+m-n) - a B (1+m+n))) \right) \right. \\ & \quad \left. (e x)^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] \right) / (2 a^3 b^2 e (1+m) n^2) \end{aligned}$$

Result (type 5, 1153 leaves):

$$\begin{aligned} & \frac{1}{2 a^3 b^2 (1+m) n^2 (a + b x^n)^2} \\ & x (e x)^m \left(a^2 A b^2 c (1+m) n - a^3 b B c (1+m) n - a^3 A b d (1+m) n + a^4 B d (1+m) n - \right. \\ & \quad a A b^2 c (1+m) (a + b x^n) + a^2 b B c (1+m) (a + b x^n) + a^2 A b d (1+m) (a + b x^n) - \\ & \quad a^3 B d (1+m) (a + b x^n) - a A b^2 c m (1+m) (a + b x^n) + a^2 b B c m (1+m) (a + b x^n) + \\ & \quad a^2 A b d m (1+m) (a + b x^n) - a^3 B d m (1+m) (a + b x^n) + 2 a A b^2 c (1+m) n (a + b x^n) - \\ & \quad \left. 2 a^3 B d (1+m) n (a + b x^n) + A b^2 c (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \right. \\ & \quad a b B c (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\ & \quad a A b d (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\ & \quad a^2 B d (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\ & \quad 2 A b^2 c m (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\ & \quad 2 a b B c m (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\ & \quad \left. 2 a A b d m (a + b x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \right. \end{aligned}$$

$$\begin{aligned}
 & 2 a^2 B d m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & A b^2 c m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a b B c m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a A b d m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 B d m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 3 A b^2 c n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a b B c n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a A b d n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 B d n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 3 A b^2 c m n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a b B c m n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a A b d m n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 B d m n (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 A b^2 c n^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right]
 \end{aligned}$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (A+B x^n) (c+d x^n)^2}{(a+b x^n)^3} dx$$

Optimal (type 5, 322 leaves, 4 steps):

$$\begin{aligned}
 & \frac{(d (b c (1+m) - a d (1+m+n)) (A b (1+m) - a B (1+m+2 n)) (e x)^{1+m}) / (2 a^2 b^3 e (1+m) n^2) +}{2 a b e n (a+b x^n)^2} \\
 & \frac{((b c - a d) (e x)^{1+m} (c (a B (1+m) - A b (1+m-2 n)) - d (A b (1+m) - a B (1+m+2 n)) x^n)) /}{(2 a^2 b^2 e n^2 (a+b x^n)) + ((b c (a B (1+m) - A b (1+m-2 n)) (a d (1+m) - b c (1+m-n)) -} \\
 & \quad a d (b c (1+m) - a d (1+m+n)) (A b (1+m) - a B (1+m+2 n)))} \\
 & (e x)^{1+m} \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] \Big/ (2 a^3 b^3 e (1+m) n^2)
 \end{aligned}$$

Result (type 5, 1924 leaves):

1

$$2 a^3 b^3 (1+m) n^2 (a+b x^n)^2$$

$$\begin{aligned}
 & x (e x)^m \left(a^2 A b^3 c^2 (1+m) n - a^3 b^2 B c^2 (1+m) n - 2 a^3 A b^2 c d (1+m) n + 2 a^4 b B c d (1+m) n + \right. \\
 & a^4 A b d^2 (1+m) n - a^5 B d^2 (1+m) n - a A b^3 c^2 (1+m) (a+b x^n) + a^2 b^2 B c^2 (1+m) (a+b x^n) + \\
 & 2 a^2 A b^2 c d (1+m) (a+b x^n) - 2 a^3 b B c d (1+m) (a+b x^n) - a^3 A b d^2 (1+m) (a+b x^n) + \\
 & a^4 B d^2 (1+m) (a+b x^n) - a A b^3 c^2 m (1+m) (a+b x^n) + a^2 b^2 B c^2 m (1+m) (a+b x^n) + \\
 & 2 a^2 A b^2 c d m (1+m) (a+b x^n) - 2 a^3 b B c d m (1+m) (a+b x^n) - a^3 A b d^2 m (1+m) (a+b x^n) + \\
 & a^4 B d^2 m (1+m) (a+b x^n) + 2 a A b^3 c^2 (1+m) n (a+b x^n) - 4 a^3 b B c d (1+m) n (a+b x^n) - \\
 & 2 a^3 A b d^2 (1+m) n (a+b x^n) + 4 a^4 B d^2 (1+m) n (a+b x^n) + 2 a^3 B d^2 n^2 (a+b x^n)^2 + \\
 & A b^3 c^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a b^2 B c^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 2 a A b^2 c d (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a^2 b B c d (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 A b d^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a^3 B d^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 A b^3 c^2 m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 2 a b^2 B c^2 m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 4 a A b^2 c d m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 4 a^2 b B c d m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a^2 A b d^2 m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 2 a^3 B d^2 m (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & A b^3 c^2 m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a b^2 B c^2 m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 2 a A b^2 c d m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a^2 b B c d m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 A b d^2 m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & a^3 B d^2 m^2 (a+b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 3 A b^3 c^2 n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a b^2 B c^2 n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a A b^2 c d n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a^2 b B c d n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 A b d^2 n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 3 a^3 B d^2 n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 3 A b^3 c^2 m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a b^2 B c^2 m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a A b^2 c d m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 a^2 b B c d m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & a^2 A b d^2 m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 3 a^3 B d^2 m n (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & 2 A b^3 c^2 n^2 (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & 2 a^3 B d^2 n^2 (a + b x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right]
 \end{aligned}$$

Problem 35: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n)^3 (c + d x^n)^2} dx$$

Optimal (type 5, 567 leaves, 7 steps):

$$\begin{aligned}
 & \left(d (a B c (b c (1+m) - a d (1+m-6n)) + A (a b c d (1+m-6n) - b^2 c^2 (1+m-2n) - 2 a^2 d^2 n) \right) \\
 & (e x)^{1+m} / \left(2 a^2 c (b c - a d)^3 e n^2 (c + d x^n) \right) + \frac{(A b - a B) (e x)^{1+m}}{2 a (b c - a d) e n (a + b x^n)^2 (c + d x^n)} + \\
 & \left((a B (b c (1+m) - a d (1+m-3n)) + A b (a d (1+m-5n) - b c (1+m-2n)) \right) (e x)^{1+m} / \\
 & \left(2 a^2 (b c - a d)^2 e n^2 (a + b x^n) (c + d x^n) \right) + \\
 & \left(b (a B (2 a b c d (1+m) (1+m-3n) - b^2 c^2 (1+m) (1+m-n) - \right. \\
 & \quad \left. a^2 d^2 (1+m^2 + m (2-5n) - 5n + 6n^2)) + A b (b^2 c^2 (1+m^2 + m (2-3n) - 3n + 2n^2) - \right. \\
 & \quad \left. 2 a b c d (1+m^2 + m (2-5n) - 5n + 4n^2) + a^2 d^2 (1+m^2 + m (2-7n) - 7n + 12n^2)) \right) (e x)^{1+m} \\
 & \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] / \left(2 a^3 (b c - a d)^4 e (1+m) n^2 \right) + \\
 & \left(d^2 (b c (A d (1+m-4n) - B c (1+m-3n)) + a d (B c (1+m) - A d (1+m-n))) \right) (e x)^{1+m} \\
 & \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] / \left(c^2 (b c - a d)^4 e (1+m) n \right)
 \end{aligned}$$

Result (type 5, 2176 leaves):

$$\begin{aligned}
 & \frac{1}{2 a^3 c^2 (b c - a d)^4 (1+m) n^2 (a + b x^n)^2 (c + d x^n)} \\
 & x (e x)^m \left(2 a^3 c d^2 (b c - a d) (B c - A d) (1+m) n (a + b x^n)^2 + \right. \\
 & \quad a^2 b (A b - a B) c^2 (b c - a d)^2 (1+m) n (c + d x^n) + a b c^2 (-b c + a d) (1+m) \\
 & \quad (a B (-b c (1+m) + a d (1+m-4n)) + A b (-a d (1+m-6n) + b c (1+m-2n))) (a + b x^n) \\
 & \quad (c + d x^n) + A b^4 c^4 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & \quad a b^3 B c^4 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & \quad 2 a A b^3 c^3 d (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & \quad 2 a^2 b^2 B c^3 d (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & \quad a^2 A b^2 c^2 d^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & \quad a^3 b B c^2 d^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & \quad 2 A b^4 c^4 m (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & \quad 2 a b^3 B c^4 m (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
 & \quad 4 a A b^3 c^3 d m (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & \quad 4 a^2 b^2 B c^3 d m (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
 & \quad 2 a^2 A b^2 c^2 d^2 m (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] -
 \end{aligned}$$

$$\begin{aligned}
& 2 a^3 b B c^2 d^2 m (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& A b^4 c^4 m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& a b^3 B c^4 m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 2 a A b^3 c^3 d m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 2 a^2 b^2 B c^3 d m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& a^2 A b^2 c^2 d^2 m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& a^3 b B c^2 d^2 m^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 3 A b^4 c^4 n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& a b^3 B c^4 n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 10 a A b^3 c^3 d n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 6 a^2 b^2 B c^3 d n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 7 a^2 A b^2 c^2 d^2 n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 5 a^3 b B c^2 d^2 n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 3 A b^4 c^4 m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& a b^3 B c^4 m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 10 a A b^3 c^3 d m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 6 a^2 b^2 B c^3 d m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 7 a^2 A b^2 c^2 d^2 m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 5 a^3 b B c^2 d^2 m n (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 2 A b^4 c^4 n^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 8 a A b^3 c^3 d n^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] + \\
& 12 a^2 A b^2 c^2 d^2 n^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \\
& 6 a^3 b B c^2 d^2 n^2 (a+b x^n)^2 (c+d x^n) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] +
\end{aligned}$$

$$2 a^3 d^2 n (b c (A d (1+m-4 n) - B c (1+m-3 n)) + a d (B c (1+m) + A d (-1-m+n))) \\ (a+b x^n)^2 (c+d x^n) \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]$$

Problem 36: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (a+b x^n)^2 (A+B x^n)}{(c+d x^n)^3} dx$$

Optimal (type 5, 322 leaves, 4 steps):

$$\frac{b (a d (1+m) - b c (1+m+n)) (A d (1+m) - B c (1+m+2 n)) (e x)^{1+m}}{2 c^2 d^3 e (1+m) n^2} - \\ \frac{(B c - A d) (e x)^{1+m} (a+b x^n)^2}{2 c d e n (c+d x^n)^2} - \\ \left((b c - a d) (e x)^{1+m} (a (B c (1+m) - A d (1+m-2 n)) - b (A d (1+m) - B c (1+m+2 n)) x^n) \right) / \\ \left(2 c^2 d^2 e n^2 (c+d x^n) \right) + \left((a d (B c (1+m) - A d (1+m-2 n)) (b c (1+m) - a d (1+m-n)) - \right. \\ \left. b c (a d (1+m) - b c (1+m+n)) (A d (1+m) - B c (1+m+2 n)) \right) \\ (e x)^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] / (2 c^3 d^3 e (1+m) n^2)$$

Result (type 5, 1924 leaves):

$$\frac{1}{2 c^3 d^3 (1+m) n^2 (c+d x^n)^2} \\ x (e x)^m \left(-b^2 B c^5 (1+m) n + A b^2 c^4 d (1+m) n + 2 a b B c^4 d (1+m) n - 2 a A b c^3 d^2 (1+m) n - \right. \\ a^2 B c^3 d^2 (1+m) n + a^2 A c^2 d^3 (1+m) n + b^2 B c^4 (1+m) (c+d x^n) - A b^2 c^3 d (1+m) (c+d x^n) - \\ 2 a b B c^3 d (1+m) (c+d x^n) + 2 a A b c^2 d^2 (1+m) (c+d x^n) + a^2 B c^2 d^2 (1+m) (c+d x^n) - \\ a^2 A c d^3 (1+m) (c+d x^n) + b^2 B c^4 m (1+m) (c+d x^n) - A b^2 c^3 d m (1+m) (c+d x^n) - \\ 2 a b B c^3 d m (1+m) (c+d x^n) + 2 a A b c^2 d^2 m (1+m) (c+d x^n) + a^2 B c^2 d^2 m (1+m) (c+d x^n) - \\ a^2 A c d^3 m (1+m) (c+d x^n) + 4 b^2 B c^4 (1+m) n (c+d x^n) - 2 A b^2 c^3 d (1+m) n (c+d x^n) - \\ \left. 4 a b B c^3 d (1+m) n (c+d x^n) + 2 a^2 A c d^3 (1+m) n (c+d x^n) + 2 b^2 B c^3 n^2 (c+d x^n)^2 - \right. \\ b^2 B c^3 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\ A b^2 c^2 d (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\ 2 a b B c^2 d (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\ 2 a A b c d^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\ a^2 B c d^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\ \left. a^2 A d^3 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\begin{aligned}
 & 2 b^2 B c^3 m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 A b^2 c^2 d m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 4 a b B c^2 d m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 4 a A b c d^2 m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 a^2 B c d^2 m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a^2 A d^3 m (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & b^2 B c^3 m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & A b^2 c^2 d m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a b B c^2 d m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 a A b c d^2 m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & a^2 B c d^2 m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^2 A d^3 m^2 (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 b^2 B c^3 n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & A b^2 c^2 d n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a b B c^2 d n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a A b c d^2 n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^2 B c d^2 n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 a^2 A d^3 n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 b^2 B c^3 m n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & A b^2 c^2 d m n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a b B c^2 d m n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a A b c d^2 m n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^2 B c d^2 m n (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 3 a^2 A d^3 m n (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 b^2 B c^3 n^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a^2 A d^3 n^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]
 \end{aligned}$$

Problem 37: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (a+b x^n) (A+B x^n)}{(c+d x^n)^3} dx$$

Optimal (type 5, 228 leaves, 3 steps):

$$\begin{aligned}
 & \frac{(b c - a d) (e x)^{1+m} (A + B x^n)}{2 c d e n (c + d x^n)^2} - \\
 & \frac{((a d (A d (1+m-2 n) - B c (1+m-n)) - b c (A d (1+m) - B c (1+m+n))) (e x)^{1+m})}{(2 c^2 d^2 e n^2 (c + d x^n))} - \\
 & \frac{((A d (b c (1+m) - a d (1+m-2 n)) (1+m-n) + B c (1+m) (a d (1+m-n) - b c (1+m+n))) (e x)^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right])}{(2 c^3 d^2 e (1+m) n^2)}
 \end{aligned}$$

Result (type 5, 1153 leaves):

$$\begin{aligned}
 & \frac{1}{2 c^3 d^2 (1+m) n^2 (c+d x^n)^2} \\
 & x (e x)^m \left(b B c^4 (1+m) n - A b c^3 d (1+m) n - a B c^3 d (1+m) n + a A c^2 d^2 (1+m) n - \right. \\
 & b B c^3 (1+m) (c+d x^n) + A b c^2 d (1+m) (c+d x^n) + a B c^2 d (1+m) (c+d x^n) - \\
 & a A c d^2 (1+m) (c+d x^n) - b B c^3 m (1+m) (c+d x^n) + A b c^2 d m (1+m) (c+d x^n) + \\
 & a B c^2 d m (1+m) (c+d x^n) - a A c d^2 m (1+m) (c+d x^n) - 2 b B c^3 (1+m) n (c+d x^n) + \\
 & \left. 2 a A c d^2 (1+m) n (c+d x^n) + b B c^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right. \\
 & A b c d (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & a B c d (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a A d^2 (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 b B c^2 m (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 A b c d m (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 a B c d m (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & \left. 2 a A d^2 m (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & b B c^2 m^2 (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & A b c d m^2 (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & a B c d m^2 (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a A d^2 m^2 (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & b B c^2 n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & A b c d n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a B c d n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 a A d^2 n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & b B c^2 m n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & A b c d m n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a B c d m n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 a A d^2 m n (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a A d^2 n^2 (c + d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]
 \end{aligned}$$

Problem 40: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n)^2 (c + d x^n)^3} dx$$

Optimal (type 5, 482 leaves, 7 steps):

$$\frac{d (2 A b c - 3 a B c + a A d) (e x)^{1+m}}{2 a c (b c - a d)^2 e n (c + d x^n)^2} + \frac{(A b - a B) (e x)^{1+m}}{a (b c - a d) e n (a + b x^n) (c + d x^n)^2} -$$

$$\frac{(d (a^2 d (B c (1+m) - A d (1+m-2 n)) - a b c (B c - A d) (1+m-6 n) - 2 A b^2 c^2 n) (e x)^{1+m}) / (2 a c^2 (b c - a d)^3 e n^2 (c + d x^n)) +$$

$$(b^2 (a B (b c (1+m) - a d (1+m-3 n)) + A b (a d (1+m-4 n) - b c (1+m-n))) (e x)^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right]) / (a^2 (b c - a d)^4 e (1+m) n) +$$

$$(d (b^2 c^2 (A d (1+m-4 n) - B c (1+m-2 n)) (1+m-3 n) - a^2 d^2 (B c (1+m) - A d (1+m-2 n)) (1+m-n) + 2 a b c d (B c (1+m) (1+m-3 n) - A d (1+m^2+m (2-5 n) - 5 n+4 n^2))) (e x)^{1+m} \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]) / (2 c^3 (b c - a d)^4 e (1+m) n^2)$$

Result (type 5, 2178 leaves):

$$\frac{1}{2 a^2 c^3 (b c - a d)^4 (1+m) n^2 (a + b x^n) (c + d x^n)^2}$$

$$\times (e x)^m \left(-a^2 c^2 d (b c - a d)^2 (B c - A d) (1+m) n (a + b x^n) + a^2 c d (-b c + a d) (1+m) \right.$$

$$\left. (b c (A d (1+m-6 n) - B c (1+m-4 n)) + a d (B c (1+m) - A d (1+m-2 n))) \right.$$

$$\left. (a + b x^n) (c + d x^n) + 2 a b^2 (-A b + a B) c^3 (-b c + a d) (1+m) n (c + d x^n)^2 + \right.$$

$$\left. 2 b^2 c^3 (a B (b c (1+m) - a d (1+m-3 n)) + A b (a d (1+m-4 n) - b c (1+m-n))) \right.$$

$$\left. n (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right] - \right.$$

$$\left. a^2 b^2 B c^3 d (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.$$

$$\left. a^2 A b^2 c^2 d^2 (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.$$

$$\left. 2 a^3 b B c^2 d^2 (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\left. 2 a^3 A b c d^3 (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\left. a^4 B c d^3 (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.$$

$$\left. a^4 A d^4 (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\left. 2 a^2 b^2 B c^3 d m (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.$$

$$\left. 2 a^2 A b^2 c^2 d^2 m (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \right.$$

$$\left. 4 a^3 b B c^2 d^2 m (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\left. 4 a^3 A b c d^3 m (a + b x^n) (c + d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \right.$$

$$\begin{aligned}
 & 2 a^4 B c d^3 m (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a^4 A d^4 m (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & a^2 b^2 B c^3 d m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^2 A b^2 c^2 d^2 m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 2 a^3 b B c^2 d^2 m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 2 a^3 A b c d^3 m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & a^4 B c d^3 m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^4 A d^4 m^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 5 a^2 b^2 B c^3 d n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 7 a^2 A b^2 c^2 d^2 n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 6 a^3 b B c^2 d^2 n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 10 a^3 A b c d^3 n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^4 B c d^3 n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 a^4 A d^4 n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 5 a^2 b^2 B c^3 d m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 7 a^2 A b^2 c^2 d^2 m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 6 a^3 b B c^2 d^2 m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 10 a^3 A b c d^3 m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & a^4 B c d^3 m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 3 a^4 A d^4 m n (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 6 a^2 b^2 B c^3 d n^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] + \\
 & 12 a^2 A b^2 c^2 d^2 n^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] - \\
 & 8 a^3 A b c d^3 n^2 (a+b x^n) (c+d x^n)^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right] +
 \end{aligned}$$

$$2 a^4 A d^4 n^2 (a+b x^n) (c+d x^n)^2 \text{Hypergeometric2F1}\left[1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int (e x)^m (a+b x^n)^p (A+B x^n) (c+d x^n)^q dx$$

Optimal (type 6, 211 leaves, 7 steps):

$$\frac{1}{e(1+m)} A (e x)^{1+m} (a+b x^n)^p \left(1+\frac{b x^n}{a}\right)^{-p} (c+d x^n)^q \left(1+\frac{d x^n}{c}\right)^{-q}$$

$$\text{AppellF1}\left[\frac{1+m}{n}, -p, -q, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \frac{1}{1+m+n} B x^{1+n} (e x)^m (a+b x^n)^p$$

$$\left(1+\frac{b x^n}{a}\right)^{-p} (c+d x^n)^q \left(1+\frac{d x^n}{c}\right)^{-q} \text{AppellF1}\left[\frac{1+m+n}{n}, -p, -q, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right]$$

Result (type 6, 458 leaves):

$$\frac{1}{1+m+n} a c x (e x)^m (a+b x^n)^p (c+d x^n)^q$$

$$\left(\left(A(1+m+n)^2 \text{AppellF1}\left[\frac{1+m}{n}, -p, -q, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right]\right) / \right.$$

$$\left(\left(1+m\right)\left(a c(1+m+n) \text{AppellF1}\left[\frac{1+m}{n}, -p, -q, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \right.\right.$$

$$\left.\left.n x^n\left(b c p \text{AppellF1}\left[\frac{1+m+n}{n}, 1-p, -q, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \right.\right.$$

$$\left.\left.a d q \text{AppellF1}\left[\frac{1+m+n}{n}, -p, 1-q, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right]\right)\right) +$$

$$\left(B(1+m+2n) x^n \text{AppellF1}\left[\frac{1+m+n}{n}, -p, -q, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right]\right) /$$

$$\left(a c(1+m+2n) \text{AppellF1}\left[\frac{1+m+n}{n}, -p, -q, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \right.$$

$$\left.\left.n x^n\left(b c p \text{AppellF1}\left[\frac{1+m+2n}{n}, 1-p, -q, \frac{1+m+3n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \right.\right.$$

$$\left.\left.a d q \text{AppellF1}\left[\frac{1+m+2n}{n}, -p, 1-q, \frac{1+m+3n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right]\right)\right)$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \frac{(e x)^m (a+b x^n)^p (A+B x^n)}{c+d x^n} dx$$

Optimal (type 6, 164 leaves, 6 steps):

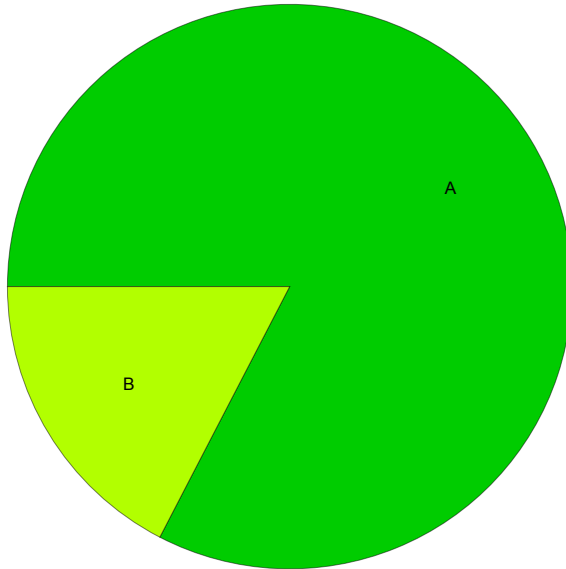
$$-\frac{1}{c d e (1+m)} (B c - A d) (e x)^{1+m} (a+b x^n)^p \left(1 + \frac{b x^n}{a}\right)^{-p} \text{AppellF1}\left[\frac{1+m}{n}, -p, 1, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + \frac{1}{d e (1+m)} B (e x)^{1+m} (a+b x^n)^p \left(1 + \frac{b x^n}{a}\right)^{-p} \text{Hypergeometric2F1}\left[\frac{1+m}{n}, -p, \frac{1+m+n}{n}, -\frac{b x^n}{a}\right]$$

Result (type 6, 438 leaves):

$$\left(a c x (e x)^m (a+b x^n)^p \left(\left(A (1+m+n)^2 \text{AppellF1}\left[\frac{1+m}{n}, -p, 1, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] \right) / \left((1+m) \left(a c (1+m+n) \text{AppellF1}\left[\frac{1+m}{n}, -p, 1, \frac{1+m+n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + n x^n \left(b c p \text{AppellF1}\left[\frac{1+m+n}{n}, 1-p, 1, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] - a d \text{AppellF1}\left[\frac{1+m+n}{n}, -p, 2, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] \right) \right) \right) + \left(B (1+m+2n) x^n \text{AppellF1}\left[\frac{1+m+n}{n}, -p, 1, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] \right) / \left(a c (1+m+2n) \text{AppellF1}\left[\frac{1+m+n}{n}, -p, 1, \frac{1+m+2n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] + n x^n \left(b c p \text{AppellF1}\left[\frac{1+m+2n}{n}, 1-p, 1, \frac{1+m+3n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] - a d \text{AppellF1}\left[\frac{1+m+2n}{n}, -p, 2, \frac{1+m+3n}{n}, -\frac{b x^n}{a}, -\frac{d x^n}{c}\right] \right) \right) \right) / ((1+m+n) (c+d x^n))$$

Summary of Integration Test Results

46 integration problems



A - 38 optimal antiderivatives

B - 8 more than twice size of optimal antiderivatives

C - 0 unnecessarily complex antiderivatives

D - 0 unable to integrate problems

E - 0 integration timeouts